POETRY OF PROGRAMMING

CLOJURE PRACTICE PROBLEMS

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These problems require relatively little work, usually just writing a function is sufficient (it is of course possible to break the solution down into several functions).

(1) Write a function capitalize-words that makes every word starting with a capital letter in a sentence given in a string.

(capitalize-words "Hello world!")
"Hello World!"
(capitalize-words "So much universe, and so little time.")
"So Much Universe, And So Little Time."

Hint: check functions in clojure.string: split, join, trim, capitalize; or use interpose, str.

(2) The *median* is the middle value of a set of (here numerical) observations, when observations are ordered. For odd number of data points, it is the middle number, for an even number it is the average of the middle two. Write a function median that takes a collection of number and returns their median.

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(median [9 1 3 8 3 5 7 8])
5
(median [2 4 5 6 1 8 2 9])
9/2
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Hint: Keep in mind that CLOJURE starts indexing from 0. Check functions: ${\tt sort}, {\tt int}.$

- (3) Write a function exp that takes two non-negative integers m and n and returns m^n .
 - (exp 2 3) 8 (exp 10 2) 100

How many multiplications does the function do in order to calculate the result? Can it be reduced? If yes, write a function fast-exp that computes the power with less multiplications! Hint: $5^{100} = 5^{50} \cdot 5^{50}$.

(4) Write a function log that takes two arguments: the base of the logarithm and a number, and computes the logarithm of the number with the given base. The function Math/log calculates the natural logarithm, and there is a formula for the change of base. If b > 0 and a, c > 0, $a, c \neq 1$, then

$$\log_a b = \frac{\log_c b}{\log_c a}.$$